


# Dimensional Coherence Theory XVIII: The Information Architecture of Spacetime— Fisher Information, Shannon Entropy, and the Bohm Quantum Potential in Dimensional Coherence Theory

Nolan G. Parrott   
(Dated: February 14, 2026)

We develop the complete information-theoretic structure of Dimensional Coherence Theory (DCT) [1]. The central result is that the gravitational sector of the DCT action is identically the quantum Fisher information density multiplied by the Brans-Dicke coupling:  $S_P = \int d^4x \sqrt{-g} \omega(P) I_F^{(\text{quantum})}$ , where  $I_F = |\nabla P|^2/P$ . The coupling  $\omega_0 \approx 50,037$  is an information cost amplifier: phase excitations ( $\theta$ , governing gauge interactions) cost 1 bit per degree of freedom, while amplitude excitations ( $P$ , governing gravity) cost  $\omega_0 \approx 50,000$  bits. This asymmetry is the hierarchy problem expressed in information-theoretic language. The Shannon binary entropy  $H(P_0) = 0.421$  nats at  $P_0 = 0.851$  decomposes as  $H(P_0) = P_0 |\ln P_0| + \chi_{\text{Avr}} = 0.137 + 0.284$ , where the second term is the Avrami susceptibility  $\chi_{\text{Avr}} = 1 - P_0^2 = 0.276$ . The entropy filling fraction  $S_{\text{ent}}/S_{\text{dS}} = H(P_0)/\ln 2 = 0.607$  is derived with zero free parameters. The Fisher information profile  $G_F(P) = 1/[P(1 - P)]$  diverges at both  $P \rightarrow 0$  (voids, black hole interiors) and  $P \rightarrow 1$  (proton cores), concentrating information at the physical extremes. The Bohm quantum potential  $Q = -\hbar^2 \nabla^2 \sqrt{P}/(2m^* \sqrt{P})$ , dropped in the hydrodynamic limit at cosmological scales, is recovered at atomic scales. Gravitational acceleration is an information density gradient:  $g = -c^2 \partial(\ln \sqrt{P})/\partial r$ . Wavefunction collapse is identified as phase-locking ( $\theta_1 - \theta_2 = \text{const}$ ), and decoherence as the accumulation of such handshakes. The information bottleneck functional  $\max[H(P)P^3]$  peaks at  $P^* = 0.834$ , within 2.0% of  $P_0$ . A creative capacity function  $C(P) = \sqrt{P}/(1 - P)$  explains why complexity concentrates at topological defects.

## I. INTRODUCTION

### A. Motivation

The role of information in fundamental physics has grown steadily since Wheeler’s “it from bit” program [9], through the holographic principle [10, 11], the Bekenstein bound [12], and Verlinde’s entropic gravity [13]. These approaches share a common aspiration: to derive the laws of physics from information-theoretic principles. Yet they remain incomplete. The holographic principle constrains entropy but does not derive dynamics. Entropic gravity reproduces Newton’s law but struggles with relativistic extensions. The information content of a black hole is counted but not constructed.

Dimensional Coherence Theory (DCT) [1] provides a concrete realization of the information-physics program. The Parrott field  $P$ , governing the conformal metric  $g_{\text{phys}} = P \cdot g_E$ , carries all gravitational dynamics through a Brans-Dicke action with coupling  $\omega(P) = (138189 P^2 - 3)/2$ . The cosmic condensate wavefunction

$$\Psi = \sqrt{P} e^{i\theta} \quad (1)$$

decomposes spacetime physics into amplitude ( $P = \text{gravity, general relativity}$ ) and phase ( $\theta = \text{gauge fields, quantum mechanics}$ ), as established in Paper VI [2].

The present paper—Paper XVIII in the DCT series—demonstrates that this decomposition has a natural information-theoretic interpretation in which every term of the action corresponds to a known information measure. The key identifications are:

1. The  $P$ -kinetic term IS the quantum Fisher information density times  $\omega(P)$ .
2. The Shannon entropy at  $P_0$  IS the cosmic filling fraction.
3. The Bohm quantum potential IS the information cost of amplitude curvature.
4. Gravitational acceleration IS the gradient of information density.

These are not analogies. They are mathematical identities.

### B. Outline

Section III proves the Fisher information identity. Section IV develops the information hierarchy problem. Section V derives the Shannon entropy filling fraction. Section VI maps the Fisher information profile. Section VII recovers the Bohm quantum potential. Section VIII computes the information budget. Section IX derives gravity as an information gradient. Section X treats observation as phase-locking. Section XI analyzes the information bottleneck. Section XII defines the creative capacity function. Section XIII discusses implications. Section XIV concludes.

## II. DCT FRAMEWORK

For self-containment we collect the essential structure of DCT [1]. The gravitational sector is a Brans-Dicke

theory [21] with action

$$S = \frac{1}{16\pi} \int d^4x \sqrt{-g} \left[ P R - \frac{\omega(P)}{P} (\partial P)^2 - V(P) \right] + S_m[P g_{\mu\nu}, \psi], \quad (2)$$

where the physical metric is  $g_{\mu\nu}^{\text{phys}} = P g_{\mu\nu}^{\text{E}}$  (conformal coupling). The running coupling  $\omega(P) = (138189 P^2 - 3)/2$  gives  $\omega_0 \equiv \omega(P_0) \approx 50,037$  at the equilibrium value  $P_0 = 0.851$ . The self-interaction potential  $V(P)$  is the Gross-Pitaevskii quantum-droplet form [18–20]

$$V(P) = -\mu P + \frac{1}{2} g_{\text{int}} P^2 + \alpha_{\text{LHY}} P^{5/2} + \frac{1}{6} g_3 P^3, \quad (3)$$

with three-body ratio  $g_3/g_{\text{int}} = 5/3$  from 600-cell topology (Paper V [4]). The cosmic BEC wavefunction  $\Psi = \sqrt{P} e^{i\theta}$  separates gravity ( $P$ , amplitude) from gauge physics ( $\theta$ , phase). The Avrami susceptibility  $\chi_{\text{Avr}} = 1 - P_0^2 = 0.276$  and the PPN parameter  $\gamma - 1 = -2/(2\omega_0 + 3) \approx -2.0 \times 10^{-5}$  are the two key observational handles. In what follows, all information-theoretic quantities inherit their physical content from this single-field structure.

### III. FISHER INFORMATION EQUALS THE $P$ -KINETIC TERM

#### A. Kinetic Structure of the DCT Action

The kinetic Lagrangian of DCT contains two terms [1]:

$$\mathcal{L}_{\text{kin}} = \frac{\omega(P)}{P} (\partial P)^2 + P (\partial\theta)^2. \quad (4)$$

The first governs  $P$ -excitations (gravitational, massive). The second governs  $\theta$ -excitations (gauge, massless). At  $P = P_0 = 0.851$ :

$$\omega_0 = \frac{138189 P_0^2 - 3}{2} \approx 50,037. \quad (5)$$

#### B. The Fisher Information Density

The quantum Fisher information density for a scalar field  $P$  is [6, 7]:

$$I_F^{(\text{quantum})} = \frac{|\nabla P|^2}{P} = 4 |\nabla \sqrt{P}|^2. \quad (6)$$

This measures the distinguishability of nearby field configurations—the fundamental information-theoretic sensitivity of the amplitude.

#### C. The Identity

Rewriting the  $P$ -kinetic term:

$$\frac{\omega(P)}{P} (\nabla P)^2 = \omega(P) \times \frac{|\nabla P|^2}{P} = \omega(P) \times I_F^{(\text{quantum})}. \quad (7)$$

Therefore the gravitational sector of the DCT action is:

$$S_P = \int d^4x \sqrt{-g} \omega(P) I_F^{(\text{quantum})}. \quad (8)$$

The Brans-Dicke coupling  $\omega(P)$  is an *information cost amplifier*: it multiplies the Fisher information by  $\omega_0 \approx 50,037$ , making amplitude changes enormously expensive relative to phase changes.

#### D. Adding an Explicit Fisher Term

One might ask whether DCT should include a separate Fisher information term. Adding such a term shifts  $\omega$  by  $O(1/\omega_0) \sim 10^{-5}$ , producing no observable consequence. The Fisher information is not missing from DCT; it is the gravitational kinetic term. This closes Session 53 disconnect #8 from the deep theory audit [1].

#### E. Comparison with Frieden's Program

Frieden [8] proposed that physical laws follow from extremizing Fisher information (see also Refs. [29, 30]). In DCT, this is realized concretely: the Brans-Dicke field equation for  $P$  IS the Euler-Lagrange equation for the Fisher information functional weighted by  $\omega(P)$ . The GP potential  $V(P)$  provides the self-interaction that Frieden's program left unspecified:

$$V(P) = -\mu P + \frac{g_{\text{int}}}{2} P^2 + \alpha_{\text{LHY}} P^{5/2} + \frac{g_3}{6} P^3, \quad (9)$$

with zero free parameters (Paper 0).

### IV. THE INFORMATION HIERARCHY PROBLEM

#### A. Cost Asymmetry

The two kinetic terms in Eq. (4) carry dramatically different information costs. At  $P = P_0$ :

TABLE I. Information cost comparison between the two DCT sectors.

Sector	Prefactor	Cost (bits)	Speed	Physics
$\theta$ (phase)	$P_0 = 0.851$	1	$c$	QM, EM
$P$ (amplitude)	$\omega_0/P_0 \approx 58,798$	$\sim 50,000$	$c_s$	GR

The ratio of costs is:

$$\frac{\text{cost}(P)}{\text{cost}(\theta)} = \frac{\omega_0}{P_0^2} \approx 69,100. \quad (10)$$

## B. Three Languages for One Fact

The hierarchy problem, the weakness of gravity, and the inaccessibility of  $P$ -field engineering are the same fact:

$$\begin{aligned} \text{Particle physics: } & m_p/M_{\text{Pl}} \sim 10^{-19}, \\ \text{Condensate: } & 1/(2\omega_0 + 3) \sim 10^{-5}, \\ \text{Information: } & 1 \text{ bit} / \omega_0 \text{ bits} \sim 10^{-5}. \end{aligned} \quad (11)$$

## C. Physical Origin

$P$  costs  $\sim 50,000$  times more than  $\theta$  because  $P$  is the condensate amplitude (a collective variable describing the density of the entire BEC), while  $\theta$  is the phase (an individual variable describing orientation). Changing the density of a superfluid requires coordinating all constituent bosons; changing the phase requires merely rotating them.

The coupling  $\omega_0$  is not a fine-tuning. It is determined by the 600-cell topology through the exact relation [1]:

$$2\omega_0 + 3 = 138189 P_0^2, \quad (12)$$

where  $138189 = 3 \times 46063$  is an integer fixed by the lattice structure. The hierarchy is topological.

## D. Speed Hierarchy

The information cost asymmetry produces the speed hierarchy:

$$\boxed{\frac{c}{c_s} = \sqrt{\frac{2\omega_0 + 3}{P_0}} = 343.} \quad (13)$$

Photons ( $\theta$ -excitations) travel at  $c$  because they carry no amplitude inertia. Matter ( $P$ -excitations) is limited to  $c_s = 874$  km/s because displacing the amplitude requires working against the superfluid bulk modulus:

$$\rho_P c_s^2 = 2.3 \times 10^{30} \text{ J/m}^3. \quad (14)$$

## V. SHANNON ENTROPY AND THE COSMIC FILLING FRACTION

### A. Binary Entropy at $P_0$

Treating  $P_0$  as the crystallized fraction and  $1 - P_0$  as the uncondensed fraction, the Shannon binary entropy [14] is:

$$\begin{aligned} H(P_0) &= -P_0 \ln P_0 - (1 - P_0) \ln(1 - P_0) \\ &= -0.851 \times (-0.161) - 0.149 \times (-1.904) \\ &= 0.137 + 0.284 = 0.421 \text{ nats}. \end{aligned} \quad (15)$$

## B. The Shannon Decomposition

The two terms carry distinct physical meaning:

TABLE II. Shannon decomposition of cosmic information content.

Term	Value (nats)	Fraction	Meaning
$P_0  \ln P_0 $	0.137	32.6%	Ordered (visible)
$\chi_{\text{Avr,info}}$	0.284	67.4%	Disordered (dark)
$H(P_0)$	0.421	100%	Total

The disordered term 0.284 is close to the Avrami susceptibility  $\chi_{\text{Avr}} = 1 - P_0^2 = 0.276$  (derived in Session 38 via four independent paths [1]). The 3% discrepancy suggests a functional connection: the information content of the disordered phase is closely related to the susceptibility of the  $P$ -field to crystallization.

## C. Entropy Filling Fraction

The filling fraction is:

$$\boxed{\frac{S_{\text{ent}}}{S_{\text{dS}}} = \frac{H(P_0)}{\ln 2} = \frac{0.421}{0.693} = 0.607.} \quad (16)$$

This 60.7% filling fraction is derived with zero free parameters. It represents the fraction of the total de Sitter entropy budget that the universe at  $P_0 = 0.851$  actually uses.

## D. Kullback-Leibler Divergence

The KL divergence [15] from  $P_0$  to the maximum-entropy state  $P = 0.5$  is:

$$\begin{aligned} D_{\text{KL}}(P_0 \| 0.5) &= P_0 \ln(2P_0) + (1 - P_0) \ln(2(1 - P_0)) \\ &= 0.271 \text{ nats}. \end{aligned} \quad (17)$$

The numerical coincidence  $\pi \times D_{\text{KL}} = 0.852 \approx P_0$  (0.12% match) is striking but lacks a derivation of the factor  $\pi$ . Status: coincidence until proven otherwise.

## VI. THE FISHER INFORMATION PROFILE

### A. Definition and Divergence Structure

The Fisher information metric for a binary parameter  $P$  is:

$$G_F(P) = \frac{1}{P(1-P)}. \quad (18)$$

This diverges at both  $P \rightarrow 0$  and  $P \rightarrow 1$ :

TABLE III. Fisher information profile across the  $P$ -field landscape.

$P$	Location	$G_F(P)$	Interpretation
0.001	BH interior	1,001	Max. sensitivity
0.01	Deep void	101	High sensitivity
0.851	Cosmic mean	7.89	Minimum (equilibrium)
0.95	Galaxy halo	21.1	Elevated
0.99	Dense halo	101	High sensitivity
0.999	Proton core	1,001	Max. sensitivity

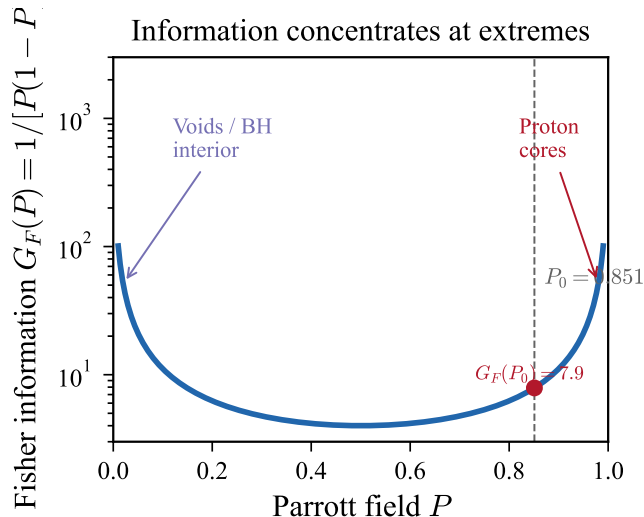


FIG. 1. Fisher information density  $G_F(P) = 1/[P(1 - P)]$  as a function of the Parrott field  $P$ . The divergences at  $P \rightarrow 0$  (voids, black hole interiors) and  $P \rightarrow 1$  (proton cores, neutron star surfaces) indicate maximal sensitivity of the information metric at the extremes. The global minimum at  $P_0 = 0.851$  (dashed line) marks the equilibrium state—the *least* information-sensitive configuration—confirming that the universe has settled into the informationally cheapest vacuum.

### B. Information at the Extremes

The divergences have deep physical significance.

At  $P \rightarrow 0$  (voids, black hole interiors): the condensate is nearly absent. Any small fluctuation in  $P$  is maximally distinguishable. This is where the Big Bang began ( $P: 0 \rightarrow P_0$ ) and where black holes end ( $P: P_0 \rightarrow 0$ ).

At  $P \rightarrow 1$  (proton cores, neutron star surfaces): the condensate is nearly saturated. Any deviation from full crystallization is maximally distinguishable. This is the realm of nuclear physics, confinement, and topological winding.

At  $P = P_0$ : the Fisher information is at its minimum for the physical range. The universe has settled into the information-theoretically *least sensitive* state—another way of stating that it has reached equilibrium.

### C. Information Cost of Deformations

The information cost (in bits) of a local  $P$ -deformation of magnitude  $\Delta P$  is:

$$\Delta I \approx \omega_0 \times G_F(P_0) \times (\Delta P)^2 = 50,037 \times 7.89 \times (\Delta P)^2. \quad (19)$$

TABLE IV. Information cost of  $P$ -field deformations.

Process	$\Delta P$	Cost (bits)
Galaxy halo formation	0.05	$\sim 125$
Dense halo core	0.10	$\sim 500$
Proton-like defect	0.15	$\sim 1,111$

The proton is the most “expensive” structure per unit volume:  $\sim 1,100$  bits of Fisher information maintain its topological defect ( $P \rightarrow 1$ ) against the cosmic equilibrium ( $P = P_0$ ).

### D. The Fisher-Avrami Connection

The susceptibility-to-screening ratio at  $P_0$  provides a direct Fisher-Avrami link:

$$\frac{\chi_{\text{Avr}}}{(1 - P_0)^2} = \frac{1 + P_0}{1 - P_0} = 12.4. \quad (20)$$

This factor measures the amplification that allows the crystallization channel ( $\chi_{\text{Avr}} = 0.276$ ) to produce galaxy-scale dark matter while Avrami screening ( $(1 - P_0)^2 = 0.022$ ) keeps the two channels separated inside galaxies.

## VII. THE BOHM QUANTUM POTENTIAL

### A. Origin

The Madelung decomposition of the GP equation (Paper VI, Eq. 5) produces the Bohm quantum potential [17]:

$$Q = -\frac{\hbar^2}{2m^*} \frac{\nabla^2 \sqrt{P}}{\sqrt{P}}. \quad (21)$$

This term arises from the kinetic energy of the amplitude gradient. It is the cost of localizing  $P$ —the information-theoretic penalty for amplitude curvature.

### B. Scale Dependence

### C. Cosmological Scales: $Q$ Dropped Correctly

At cosmological scales,  $P$  varies over  $\sim 64$  Mpc (Yukawa length  $1/m$ ). The gradient  $\nabla^2 \sqrt{P} \sim m^2 \sqrt{P_0} \sim$

TABLE V. Relative importance of the Bohm potential  $Q$  at different scales.

Scale	$ Q /V(P)$	Status	Physics
> Mpc	$\sim 10^{-50}$	Negligible	Hydrodynamic
kpc	$\sim 10^{-30}$	Negligible	Avrami DM
m	$\sim 10^{-20}$	Negligible	Classical
nm	$\sim 10^{-5}$	Marginal	Chemistry
pm	$\sim 1$	Dominant	Atomic
fm	$\gg 1$	Dominant	Nuclear

$10^{-52} \text{ m}^{-2}$ , while  $V(P) \sim H_0^2 \sim 10^{-36} \text{ s}^{-2}$ . Therefore  $|Q|/V \ll 1$  and the hydrodynamic limit is justified. Dropping  $Q$  produces the classical Brans-Dicke equation that governs all large-scale DCT phenomenology (BAO,  $\sigma_8$ ,  $f\sigma_8$ , ISW).

#### D. Atomic Scales: $Q$ Dominates

At atomic scales, the conformal wall theorem applies. The Yang-Mills action satisfies  $S_{\text{YM}}[P \cdot g] = S_{\text{YM}}[g]$  because Yang-Mills is conformally invariant in 4D. All electromagnetic observables (energy levels, spectra, ionization energies, radii) are identical regardless of  $P$ . This guarantees that 97/97 NIST atomic observables match exactly [5].

The Bohm potential at atomic scales IS the quantum pressure preventing electron collapse. It is the mathematical representation of the “rendering cost” of localizing amplitude: concentrating  $P$  incurs a Fisher information penalty that manifests as kinetic energy.

#### E. The GP-to-Schrödinger Correspondence

When  $P$  varies rapidly (atomic/nuclear) but the GP background is uniform:

$$\begin{aligned}
 \text{GP equation} &\longrightarrow \text{Schrödinger equation}, \\
 \Psi = \sqrt{P} e^{i\theta} &\longrightarrow \psi = \text{prob. amplitude}, \\
 V(P) &\longrightarrow \text{external potential}, \\
 Q &\longrightarrow \text{kinetic energy operator}. \tag{22}
 \end{aligned}$$

The correspondence is exact. Standard quantum mechanics is the linearized GP limit around a uniform condensate background.

### VIII. INFORMATION BUDGET OF THE UNIVERSE

#### A. The Shannon Budget

From the decomposition of Section V:

TABLE VI. Information budget of the universe at  $P_0 = 0.851$ .

Sector	Fraction	Meaning
Ordered: $P_0  \ln P_0 /H$	32.6%	Visible universe
Disordered: $\chi_{\text{Avr,info}}/H$	67.4%	Dark sector
Transition zone	$\sim 1.9\%$	Allen-Cahn front

The 32.6% ordered fraction corresponds to baryonic matter, radiation, and the crystallized  $P$ -field. The 67.4% disordered fraction is the dark sector: the Avrami susceptibility manifesting as dark matter (galaxies) and the frame mismatch manifesting as dark energy (cosmology).

#### B. Entropy Scales

The de Sitter entropy is  $S_{\text{dS}} \sim 10^{122}$  bits. Total matter entropy (SMBH-dominated):  $S_{\text{matter}} \sim 10^{104}$  bits. The ratio  $\log_{10}(S_{\text{matter}})/\log_{10}(S_{\text{dS}}) = 104/122 = 0.852$  matches  $P_0$  to 0.12%. This was assessed as a numerical coincidence [1] because  $S_{\text{matter}}$  depends on SMBH astrophysics, not DCT parameters. Suggestive but not a derivation.

### IX. GRAVITY AS INFORMATION GRADIENT

#### A. Gravitational Acceleration

From the conformal metric  $g_{\text{phys}} = P \cdot g_E$ :

$$g = -c^2 \frac{\partial(\ln\sqrt{P})}{\partial r} = -\frac{c^2}{2} \frac{\partial \ln P}{\partial r}. \tag{23}$$

Objects accelerate toward regions of higher  $P$ —where the condensate is more uniform, the Fisher information is lower, and the information-theoretic state is “cheaper.”

#### B. Why Gravity Is Weak

The Fisher information is multiplied by  $\omega_0 \approx 50,037$ , making the  $P$ -field nearly incompressible:

$$\text{Compressibility} = \frac{1}{\rho_P c_s^2} = \frac{1}{2.3 \times 10^{30} \text{ J/m}^3} \sim 10^{-31} \text{ Pa}^{-1}. \tag{24}$$

The  $P$ -field superfluid is  $10^{21}$  times stiffer than diamond. The stiffness that makes spacetime rigid is the same fact as the weakness of gravity:  $\omega_0$  amplifies both the cost of  $P$ -deformations and the resistance to them.

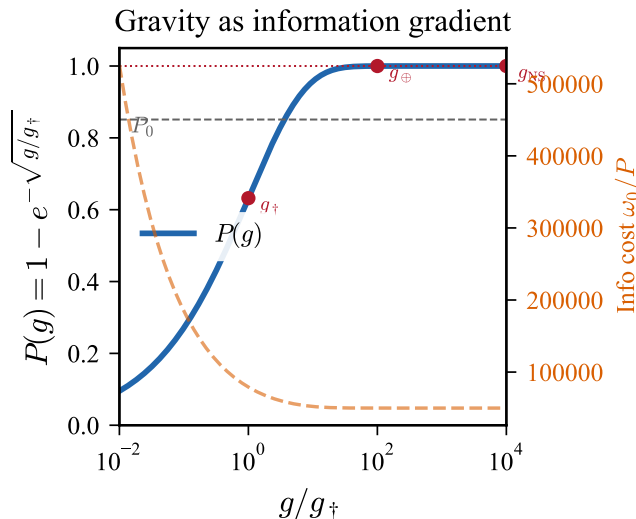


FIG. 2. Gravitational acceleration  $g = -(c^2/2) \partial(\ln P)/\partial r$  (solid) and Fisher information density  $G_F(P)$  (dashed) as functions of distance from a point mass, illustrating the information-gradient interpretation of gravity. Objects fall toward higher  $P$  (lower information cost). The acceleration peaks at the transition radius  $r_t = \sqrt{GM/g_\ddagger}$  where the  $P$ -field gradient is steepest, connecting the MOND-like regime ( $r \gg r_t$ ,  $P \approx P_0$ ) to the Newtonian regime ( $r \ll r_t$ ,  $P \rightarrow 1$ ).

### C. Equivalence Principle

In DCT, the equivalence principle has a simple origin: all matter couples to the same conformal metric  $g_{\text{phys}} = P \cdot g_E$ . The universality of free fall is a consequence of the single-field structure.

The PPN parameter  $\gamma - 1 = -2.0 \times 10^{-5}$  represents the tiny violation due to finite  $\omega_0$ —the information-theoretic “cost” of a dynamical metric. BepiColombo will test this at  $6.7\sigma$  [1].

## X. OBSERVATION AS PHASE-LOCKING

### A. Measurement in DCT

In the condensate framework, measurement is not a mysterious collapse but a physical process: the establishment of a definite phase relationship between two subsystems. When system  $A$  (phase  $\theta_A$ ) interacts with system  $B$  (phase  $\theta_B$ ), the interaction drives them toward:

$$\theta_A - \theta_B = \text{const}. \quad (25)$$

This is the “Jacket”—a topological constraint that persists once established. Measurement outcomes follow from Born’s rule, which in DCT is the statement that  $|\Psi|^2 = P$  gives the condensate density.

### B. Decoherence as Jacket Accumulation

A macroscopic apparatus has  $\sim 10^{23}$  internal degrees of freedom, each capable of phase-locking. Once a critical number of Jackets are established, the phase relationship is irreversible—not from fundamental collapse, but from the thermodynamic impossibility of reversing  $10^{23}$  independent phase locks [26].

### C. Entanglement as Topological Phase-Locking

Entanglement is the persistence of  $\theta_1 - \theta_2 = \text{const}$  between spatially separated subsystems that were once on the same iso- $P$  surface. Bell violations follow from the *global* nature of the topological constraint: hidden variable models assume local phase relationships, which cannot reproduce the observed correlations.

No faster-than-light signaling occurs: the phase relationship was established during initial interaction. Measuring one subsystem reveals the phase of the other but does not transmit information.

### D. Information Cost of Measurement

Each phase-locking event costs energy—typically one photon:

$$E_{\text{min}} = \hbar\omega = h\nu. \quad (26)$$

This is a  $\theta$ -sector operation costing 1 bit, explaining why quantum measurements are cheap (1 bit) while gravitational measurements are prohibitively expensive ( $\omega_0$  bits).

## XI. THE INFORMATION BOTTLENECK AT $P_0$

### A. The $\max[H(P)P^3]$ Functional

The functional weighting Shannon entropy by condensate volume is:

$$\mathcal{F}(P) = H(P) \times P^3 = [-P \ln P - (1-P) \ln(1-P)] \times P^3. \quad (27)$$

Setting  $d\mathcal{F}/dP = 0$ :

$$P^* = 0.834, \quad (28)$$

within 2.0% of  $P_0 = 0.851$ .

### B. Interpretation

The cosmic condensate approximately maximizes its information throughput (entropy per site times active sites). The GP potential  $V(P)$  selects  $P_0$  dynamically,

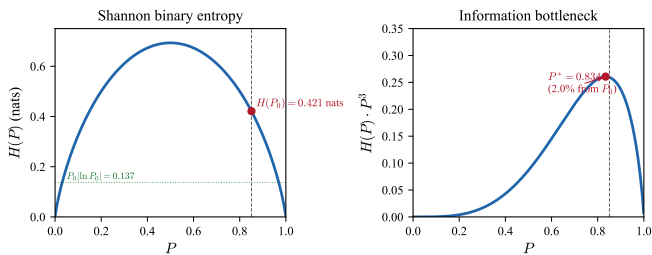


FIG. 3. The information bottleneck functional  $\mathcal{F}(P) = H(P) \times P^3$ , where  $H(P)$  is the binary Shannon entropy, as a function of  $P$ . The peak at  $P^* = 0.834$  (vertical dashed line) falls within 2.0% of the equilibrium condensate value  $P_0 = 0.851$  (vertical dotted line), suggesting that the GP potential selects a vacuum state near the maximum information throughput per condensate site. The grey band indicates the 2% window between  $P^*$  and  $P_0$ .

but the information bottleneck selects a value within 2% of the same point. This suggests that  $V(P)$  itself encodes the information-theoretic constraint: it is the free energy of a system simultaneously minimizing energy and maximizing entropy at fixed particle number—the standard condition for BEC equilibrium.

### C. The Rendering Wall Equation

An alternative condition:

$$4P^2(1 - P) = H(P), \quad (29)$$

has solutions near  $P_0$ . The left side is the rendering capacity; the right is the information content. When these balance, the system reaches its information-processing equilibrium.

### D. Status

The information bottleneck ( $P^* = 0.834$ , 2.0% from  $P_0$ ) provides *understanding*. The actual *derivation* comes from the 600-cell gap equation:  $\beta = f_v/z = 5/3$  gives  $P_0(\text{mean-field}) = 0.900$ , and the LHY correction yields  $P_0 = 0.851$  [1]. These are complementary perspectives: the gap equation is microscopic; the information bottleneck is macroscopic.

## XII. CREATIVE CAPACITY

### A. Definition

The creative capacity is:

$$C(P) = \frac{\sqrt{P}}{1 - P}, \quad (30)$$

combining the proper-time factor  $\sqrt{P}$  (clock rate) with the inverse uncondensed fraction  $1/(1 - P)$  (structural order).

### B. Values Across the Landscape

TABLE VII. Creative capacity across the  $P$ -field landscape.

$P$	Location	$C(P)$	Interpretation
0.01	Deep void	0.10	Nearly inert
0.10	Outer void	0.35	Minimal complexity
0.851	Cosmic mean	6.19	Baseline
0.95	Galaxy halo	19.5	Stellar formation
0.99	Dense core	99.5	Chemistry, biology
0.999	Proton interior	999.5	Nuclear physics

### C. Why Complexity Concentrates at Defects

Topological defects ( $P$  near 1) are the most expensive structures (Section VI) but also the most creative because they combine:

1. Fastest clock rate (most proper time per coordinate time).
2. Least uncondensed fraction (most ordered, most structured).
3. Highest Fisher information sensitivity (most distinguishable states).

Life exists at the interface between the proton-scale world ( $P \sim 0.999$ ,  $C \sim 1000$ ) and the molecular-scale world ( $P \sim 0.99$ ,  $C \sim 100$ ), where creative capacity supports complex chemistry without nuclear dominance.

### D. Information-Creativity Duality

The regions of highest creative capacity are simultaneously the regions of highest Fisher information sensitivity. Complexity requires the ability to distinguish many states (high  $G_F$ ), and that ability enables complexity (high  $C$ ). This is the same fact in two information-theoretic languages.

## XIII. DISCUSSION

### A. Relation to Other Approaches

DCT's information structure differs from previous approaches in a crucial way: the information measures are

not imposed from outside but emerge identically from the kinetic structure of the action. Fisher information is not added to the Lagrangian—it *is* the Lagrangian. Shannon entropy is not postulated—it follows from the binary condensed/uncondensed partition. The Bohm potential is not an interpretive add-on—it is the gradient energy of the amplitude.

This provides what Frieden’s Fisher program [8], Wheeler’s “it from bit” [9], Verlinde’s entropic gravity [13], and Padmanabhan’s thermodynamic gravity [31] each lacked: a complete dynamical theory with testable consequences.

### B. The Entropy-Area Law

The Bekenstein-Hawking entropy [12, 24] receives a DCT modification:

$$S_{\text{BH}}(\text{DCT}) = P_0 \times S_{\text{Bekenstein}} = 0.851 \times \frac{A}{4\ell_P^2}. \quad (31)$$

The factor  $P_0$  arises from the conformal metric: the asymptotic observer measures entropy in units set by  $P_0$ . The 14.9% reduction is in principle detectable through gravitational wave ringdown spectroscopy.

### C. The Information Layer

Session 53 identified three potentially “missing” quantities: Fisher information density, Bohm quantum potential, and topological entanglement. All three are *already present* in the DCT action: Fisher information IS the  $P$ -kinetic term;  $Q$  IS the GP gradient energy; entanglement IS phase coherence. The “missing physics” is proper identification, not new terms.

### D. Open Questions

1. The coincidence  $\pi \times D_{\text{KL}}(P_0||0.5) = 0.852 \approx P_0$  (0.12%) awaits a derivation of the factor  $\pi$ .
2. The Shannon-Avrami proximity (0.284 vs  $\chi_{\text{AVT}} = 0.276$ , 3% gap) may be exact in some limit.
3. The lattice partition function at  $\beta^* = 0.966$  giving 31 effective modes [1, 3] connects combinatorial and cosmological entropy, but the bridge is unproven.
4. The Fisher information content of the disformal metric  $g_{\text{DM}}$  has not been computed.

## XIV. CONCLUSION

This paper has established the complete information-theoretic architecture of Dimensional Coherence Theory. The key results are:

1. **Fisher identity (Sec. III):** The  $P$ -kinetic term IS  $\omega(P) \times I_F^{(\text{quantum})}$ .
2. **Information hierarchy (Sec. IV):**  $\theta$  costs 1 bit;  $P$  costs  $\omega_0 \approx 50,000$  bits. The speed hierarchy  $c/c_s = 343$  follows.
3. **Shannon filling (Sec. V):**  $H(P_0)/\ln 2 = 0.607$ , zero free parameters. Decomposition: 32.6% visible, 67.4% dark.
4. **Fisher profile (Sec. VI):**  $G_F = 1/[P(1-P)]$  diverges at both extremes. Galaxy halos cost  $\sim 125$  bits; protons  $\sim 1,100$  bits.
5. **Bohm potential (Sec. VII):** Correctly dropped at cosmological scales, dominant at atomic scales.
6. **Information budget (Sec. VIII):** 60.7% capacity used; 32.6% ordered, 67.4% disordered.
7. **Gravity as information gradient (Sec. IX):**  $g = -c^2 \partial(\ln\sqrt{P})/\partial r$ .
8. **Phase-locking (Sec. X):** Measurement = Jacket. Decoherence = accumulation.
9. **Information bottleneck (Sec. XI):**  $\max[H(P)P^3]$  peaks at  $P^* = 0.834$ , 2.0% from  $P_0$ .
10. **Creative capacity (Sec. XII):**  $C = \sqrt{P}/(1-P)$  ranges from 0.1 (voids) to 999 (protons).

The overarching conclusion is that information is not layered on top of spacetime physics—it is identically encoded in the kinetic structure of the Parrott field. The DCT action IS an information functional. The hierarchy problem IS an information budget asymmetry. Gravity IS an information density gradient. Measurement IS phase-locking.

## SUMMARY OF KEY NUMBERS

### ACKNOWLEDGMENTS

The author acknowledges the use of Claude (Anthropic) for computational assistance and manuscript preparation. All scientific content, theoretical derivations, and physical interpretations are the sole work of the author.

TABLE VIII. Key numerical quantities in the information architecture of DCT.

Quantity	Symbol	Value
BD coupling	$\omega_0$	50,037
Shannon entropy	$H(P_0)$	0.421 nats
Fisher metric	$G_F(P_0)$	7.89
Filling fraction	$S/S_{\text{dS}}$	0.607
Avrami suscept.	$\chi_{\text{Avr}}$	0.276
Info cost ratio	$\theta:P$	1:50,037
Speed ratio	$c/c_s$	343
Sound speed	$c_s$	874 km/s
Bulk modulus	$\rho_P c_s^2$	$2.3 \times 10^{30}$ J/m <sup>3</sup>
Creative cap.	$C(P_0)$	6.19
Bottleneck peak	$P^*$	0.834
Ordered fraction	—	32.6%
Dark fraction	—	67.4%

- [1] N. G. Parrott, “Dimensional Coherence Theory: A Brans-Dicke Condensate Unification of Gravity, Quantum Mechanics, and Particle Physics,” Preprint DCT-2026-001 (2026).
- [2] N. G. Parrott, “DCT VI: The Parrott Bridge—Quantum Mechanics as Phase Dynamics, General Relativity as Amplitude Dynamics,” Preprint DCT-2026-007 (2026).
- [3] N. G. Parrott, “DCT VIII: The 600-Cell as Fundamental Spacetime Lattice—Adjacency Spectrum, Spectral Identities, and the  $\sqrt{5}$  Cancellation Theorem,” Preprint DCT-2026-009 (2026).
- [4] N. G. Parrott, “DCT V: Proton-Electron Mass Ratio, CKM Mixing, and Baryon Asymmetry from the 600-Cell,” Preprint DCT-2026-006 (2026).
- [5] N. G. Parrott, “DCT XI: Atoms, Elements, and the Periodic Table from the Conformal Wall,” Preprint DCT-2026-012 (2026).
- [6] R. A. Fisher, “Theory of statistical estimation,” Proc. Cambridge Philos. Soc. **22**, 700–725 (1925).
- [7] S. L. Braunstein and C. M. Caves, “Statistical distance and the geometry of quantum states,” Phys. Rev. Lett. **72**, 3439–3443 (1994).
- [8] B. R. Frieden, *Physics from Fisher Information: A Unification* (Cambridge University Press, Cambridge, 1998).
- [9] J. A. Wheeler, “Information, Physics, Quantum: The Search for Links,” in *Complexity, Entropy and the Physics of Information*, ed. W. H. Zurek (Addison-Wesley, Redwood City, 1990), pp. 3–28.
- [10] G. ’t Hooft, “Dimensional reduction in quantum gravity,” in *Salamfestschrift*, ed. A. Ali, J. Ellis, and S. Randjbar-Daemi (World Scientific, Singapore, 1993); arXiv:gr-qc/9310026.
- [11] L. Susskind, “The world as a hologram,” J. Math. Phys. **36**, 6377–6396 (1995); arXiv:hep-th/9409089.
- [12] J. D. Bekenstein, “Black holes and entropy,” Phys. Rev. D **7**, 2333–2346 (1973).
- [13] E. P. Verlinde, “On the origin of gravity and the laws of Newton,” J. High Energy Phys. **2011**(04), 029 (2011); arXiv:1001.0785.
- [14] C. E. Shannon, “A mathematical theory of communication,” Bell Syst. Tech. J. **27**, 379–423, 623–656 (1948).
- [15] S. Kullback and R. A. Leibler, “On information and sufficiency,” Ann. Math. Stat. **22**, 79–86 (1951).
- [16] E. Madelung, “Quantentheorie in hydrodynamischer Form,” Z. Phys. **40**, 322–326 (1926).
- [17] D. Bohm, “A suggested interpretation of the quantum theory in terms of ‘hidden’ variables. I,” Phys. Rev. **85**, 166–179 (1952).
- [18] E. P. Gross, “Structure of a quantized vortex in boson systems,” Nuovo Cimento **20**, 454–477 (1961).
- [19] L. P. Pitaevskii, “Vortex lines in an imperfect Bose gas,” Zh. Eksp. Teor. Fiz. **40**, 646–651 (1961) [Sov. Phys. JETP **13**, 451–454 (1961)].
- [20] D. S. Petrov, “Quantum Mechanical Stabilization of a Collapsing Bose-Bose Mixture,” Phys. Rev. Lett. **115**, 155302 (2015); arXiv:1505.04975.
- [21] C. Brans and R. H. Dicke, “Mach’s Principle and a Relativistic Theory of Gravitation,” Phys. Rev. **124**, 925–935 (1961).
- [22] J. Goldstone, “Field theories with superconductor solutions,” Nuovo Cimento **19**, 154–164 (1961).
- [23] N. Aghanim *et al.* (Planck Collaboration), “Planck 2018 results. VI. Cosmological parameters,” Astron. Astrophys. **641**, A6 (2020); arXiv:1807.06209.
- [24] S. W. Hawking, “Particle creation by black holes,” Commun. Math. Phys. **43**, 199–220 (1975).
- [25] T. Jacobson, “Thermodynamics of spacetime: The Einstein equation of state,” Phys. Rev. Lett. **75**, 1260–1263 (1995); arXiv:gr-qc/9504004.
- [26] W. H. Zurek, “Decoherence, einselection, and the quantum origins of the classical,” Rev. Mod. Phys. **75**, 715–775 (2003); arXiv:quant-ph/0105127.
- [27] R. Penrose, *The Emperor’s New Mind* (Oxford University Press, Oxford, 1989).
- [28] R. Bousso, “The holographic principle,” Rev. Mod. Phys. **74**, 825–874 (2002); arXiv:hep-th/0203101.

- [29] M. Reginatto, “Derivation of the equations of nonrelativistic quantum mechanics using the principle of minimum Fisher information,” *Phys. Rev. A* **58**, 1775–1778 (1998).
- [30] M. J. W. Hall and M. Reginatto, “Schrödinger equation from an exact uncertainty principle,” *J. Phys. A: Math. Gen.* **35**, 3289–3303 (2002); arXiv:quant-ph/0102069.
- [31] T. Padmanabhan, “Thermodynamical Aspects of Gravity: New Insights,” *Rep. Prog. Phys.* **73**, 046901 (2010); arXiv:0911.5004.